

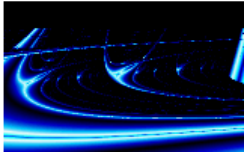
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# SOLVING PROBLEMS?

Dr A. A. Kotzé  
Financial Chaos Theory  
March 2010

**Saggitarius A\*:** supermassive black hole at the Milky Way's center





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Niels Bohr  
and  
Albert Einstein



***Before I came here I was confused about the subject. Having listened to your lecture I am still confused. But on a higher level.***

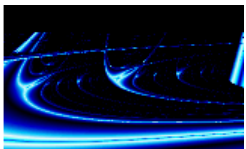
Enrico Fermi (1901-1954)

# Safex Margins

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- Safex
- [http://www.jse.co.za/DownloadFiles.aspx?RequestedNode=DownloadableDocuments/Safex/Margin\\_Requirements/2010](http://www.jse.co.za/DownloadFiles.aspx?RequestedNode=DownloadableDocuments/Safex/Margin_Requirements/2010)
- Currencies

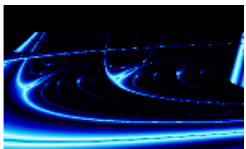
Contract Code	Expiry Date	Initial Margin Requirement	Spread Margin Requirement	VSR
Dollar/Rand (\$/R)	15 March 2010	<u>R 350.00</u>	<u>R 25.00</u>	<u>2.5</u>
Dollar/Rand (\$/R)	14 June 2010	<u>R 360.00</u>	<u>R 25.00</u>	<u>2.5</u>
Dollar/Rand (\$/R)	13 September 2010	<u>R 370.00</u>	<u>R 25.00</u>	<u>2.5</u>
Dollar/Rand (\$/R)	13 December 2010	<u>R 375.00</u>	<u>R 25.00</u>	<u>2.5</u>
Dollar/Rand (\$/R)	14 March 2011	<u>R 380.00</u>	<u>R 25.00</u>	<u>2.5</u>
Dollar/Rand (\$/R)	13 June 2011	<u>R 385.00</u>	<u>R 30.00</u>	<u>2.5</u>



## Freaking Out on Risk

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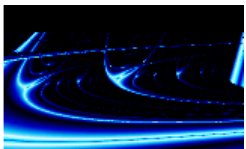
- Super Freakonomics explains what I do
- **Chapter 4: The fix is in – and it's cheap and simple**
- In the USA in 1952, 40 million cars
- Rate of death per mile driven was 5 times higher than today. Why?
- Enter Robert McNamara who believed in statistical analysis



## Car Accidents Freaking me Out

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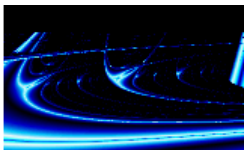
- Worked for Ford Motor Company after WWII
- Started testing with dummies
- Humans were no match for hard materials used in car interiors
- Drivers were often impaled on steering wheel
- Passengers hit the windshield or header bar of instrument panel



# First Freaking Solution

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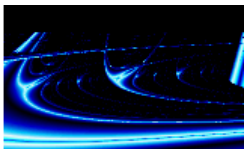
- Soften up the interior
- Worked but one can soften the steering wheel only up to point



## Better Freaking Solution

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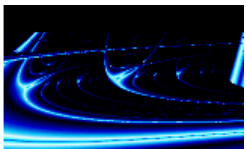
- Fit seat belts!
- Cars did not have seat belts before the mid fifties
- McNamara knew airplanes had seat belts
- Started to fit them to Ford cars – not a new solution
- Seat belts reduce the risk of death by as much as 70%



## Most Cost-Effective Freaking Solution

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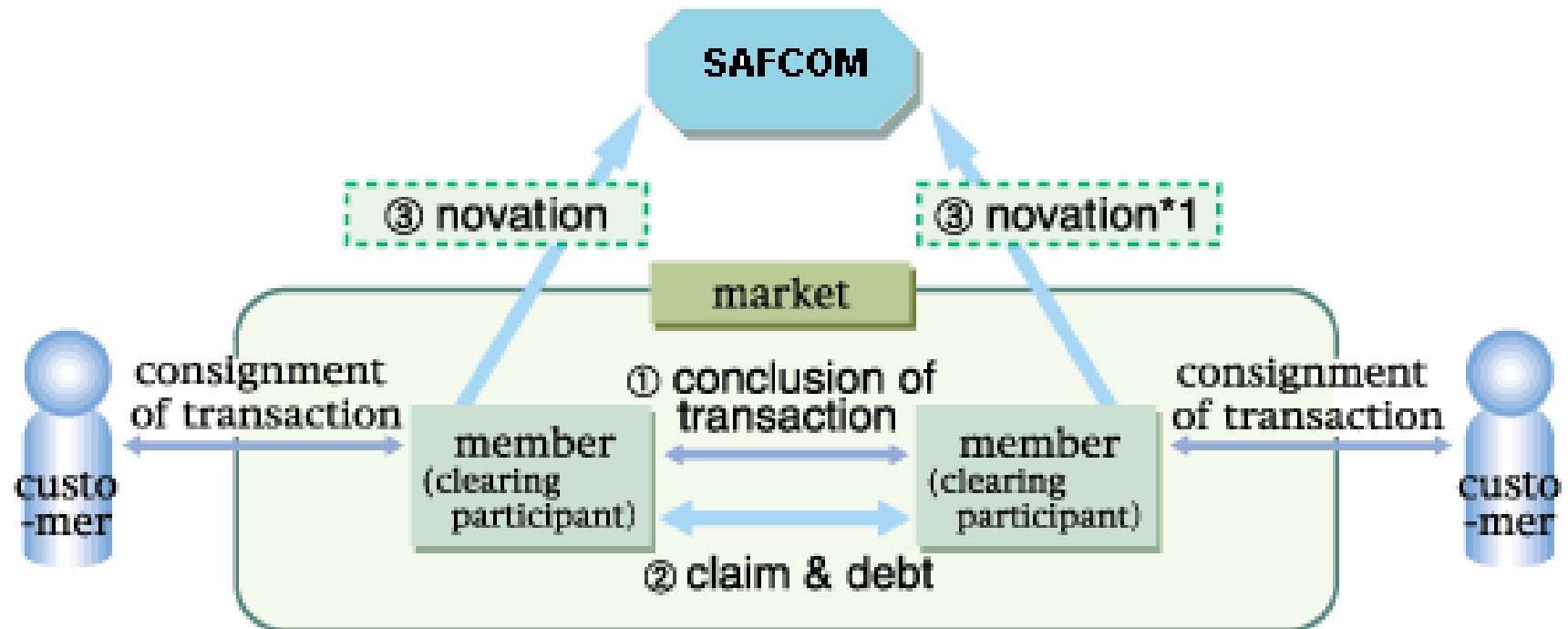
- Enter the air bag
- Cost: \$1.8 million per life saved
  
- What about seat belts?
- Cost: \$30,000 per life saved!
  
- Which solution is the best?



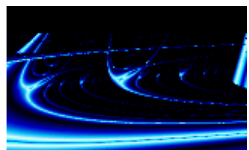


# Who Bears the Risk in a Derivatives Market?

- Clearing Houses



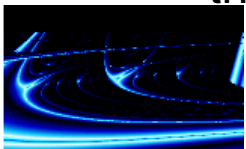
***SAFCOM bears credit risk***



# Initial Margin

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- Exchanges employ a system of margining. Accordingly, a counterparty to a transaction on an exchange is required to pay a sum over to it at the inception of the derivative transaction to cover any potential losses arising from a default – initial margin
- **Risk management** may be defined as identifying the risk of loss in a portfolio and ensuring that the **losses can be borne**.
- A futures contract's Initial Margin Requirement (IMR) is equal to the profit or loss arising from the **maximum anticipated** up or down move in its price **from one day to the next**
- It is in essence a 1 day Value at Risk (VAR) measure. It is given in Rands per futures contract.
- Should the losses eventuate and the participant be unable to bear them, the margin is available to the exchange to meet the shortfall.



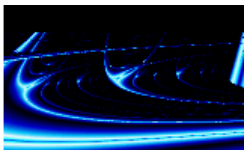
## The Risk Parameter

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- The exchange estimates this possible 1 day loss through a statistical analysis of historical market returns
- Use 751/2001 daily closing values to obtain 750/2000 daily returns
- The risk parameter is set at **3.5** Standard Deviations confidence level of 99.95%.
- Meaning? 99.95% of all possible daily changes in the market will be covered by the IMR

OR

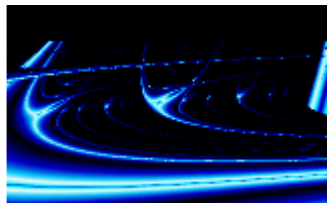
- The IMR will be enough to cover any 1 day loss 99.95% of the time
- 99.95% confidence => one loss in 2000



# The Risk Parameters

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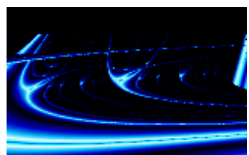
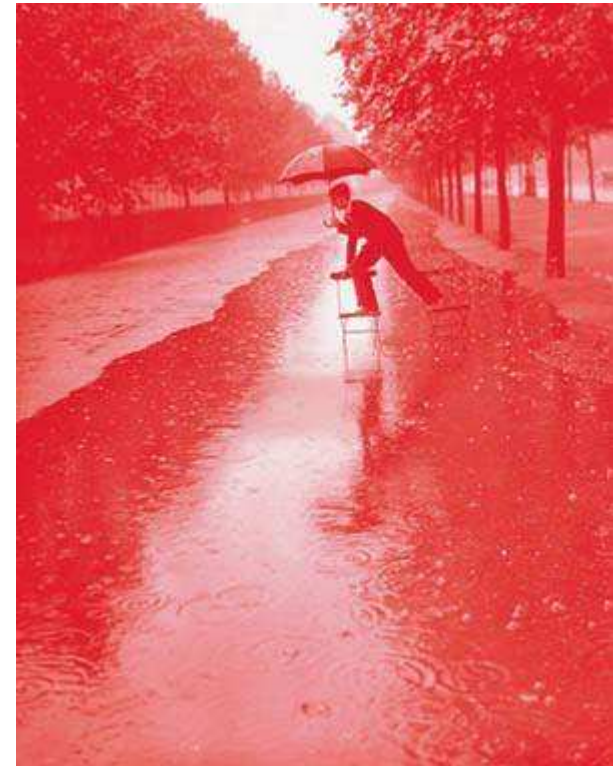
<b>Standard Deviations</b>	<b>Confidence Level</b>
$\sigma$	68.2689492137%
$1.645\sigma$	90.0000000000%
$1.96\sigma$	95.0000000000%
$2\sigma$	95.4499736104%
$2.33\sigma$	98.0000000000%
$2.576\sigma$	99.0000000000%
$3\sigma$	99.7300203937%
$3.5\sigma$	99.9500000000%
$4\sigma$	99.9936657516%
$5\sigma$	99.9999426697%
$6\sigma$	99.999998027%
$7\sigma$	99.999999997%



# Currency Futures

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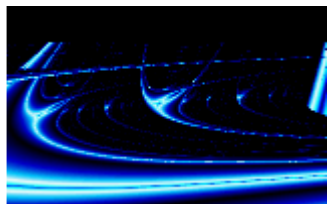
- Started trading in June 2007
- Standard Bank and Investec were liquidity providers
- New instruments – they were “weary”
- Asked YieldX to calculate margins using 6 standard deviations
- Let’s untie the risks.....excel



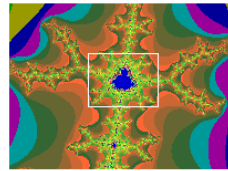
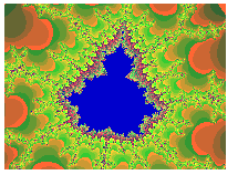
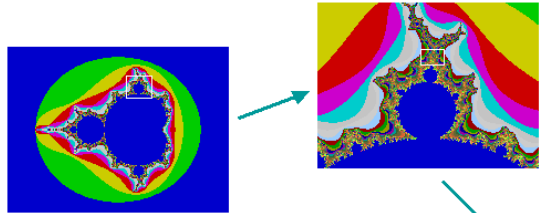
# Global Exchanges

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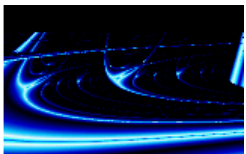
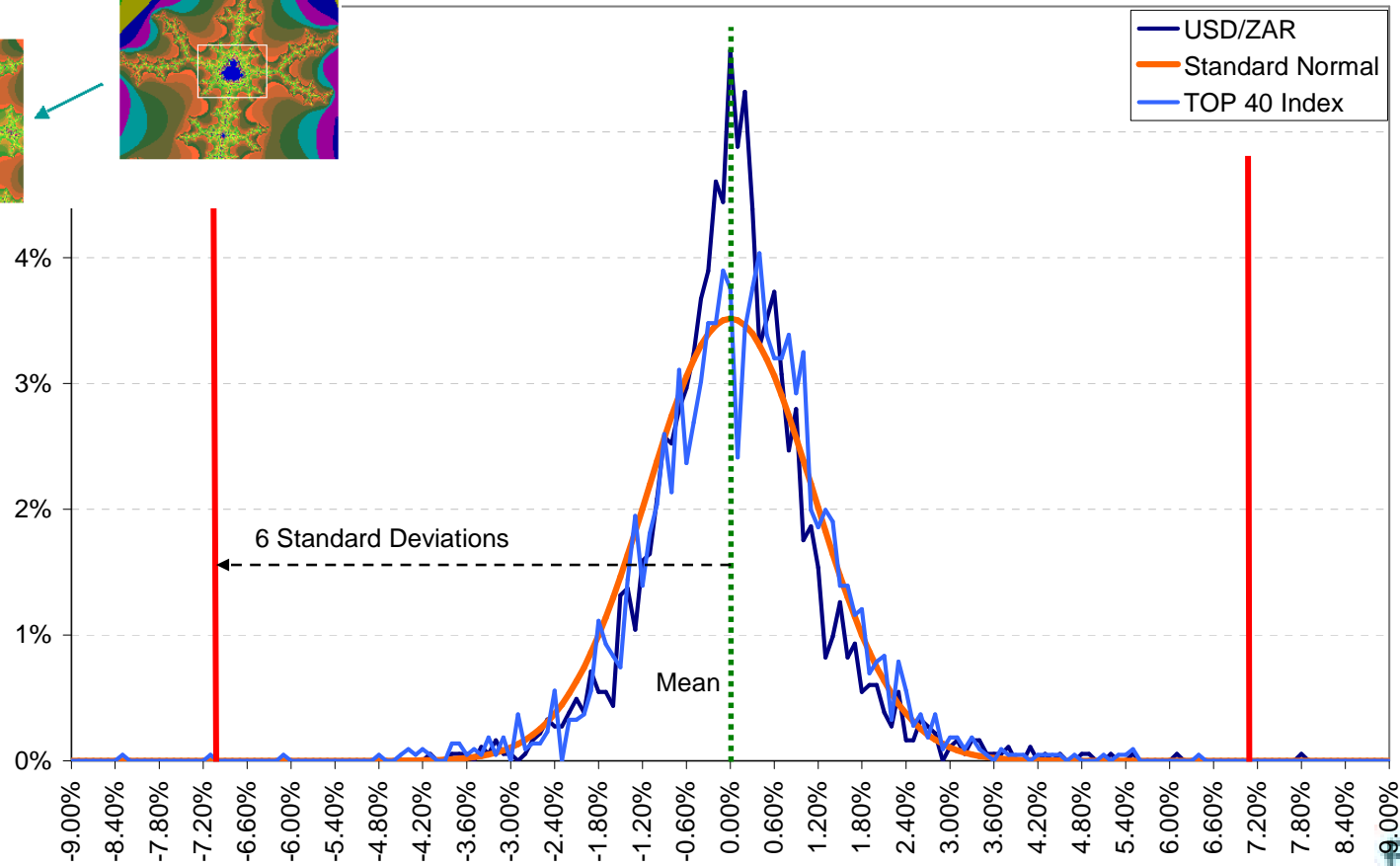
Exchange/Clearing House	Confidence Level	Standard Deviations
Natural Gas Exchange (NGX)	99.70%	3.0
Australia Securities Exchange	99.00%	2.576
LCH.Clearnet	99.70%	3.0
Bombay Stock Exchange	99.00%	2.576
X-Clear (Swiss)	99.00%	2.576
<b>Safex ED</b>	<b>99.95%</b>	<b>3.5</b>
<b>Yield-X (interest rate futures)</b>	<b>99.95%</b>	<b>3.5</b>
<b>Yield-X (currency futures)</b>	<b>9.999999%</b>	<b>6</b>



# Standard Deviation



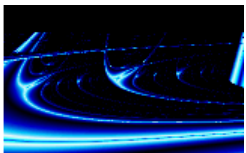
Return Distributions



# Problem 1

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- **At 6 STDEVs, margins too high and traders traded single stock futures instead**
- Let's unpack risks further..... and compare against what we are comfortable with..... and we'll also get closer to the market's view on risk.....excel
- Solution: Market did not understand the risk. A simple analysis was enough to solve this problem

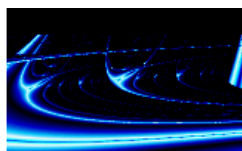




## Single Stocks and Crises of October 2008: Problem 2

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- Lehmans – no problems with SA book
- Dealstream and Cortex – SSF undermargined
- The credit crises showed that we had to enhance the model for **illiquid instruments** and **concentrated positions**
- Let's see the effect of liquidity - excel
- Concentration risk lies in the fact that a single or few parties may hold large positions relative to the issued share capital.
- Ratings of 1 & 2 are considered as Liquid Contracts – SSF will be listed
- Ratings of 3 are considered as Illiquid Contracts – SSF will not be listed

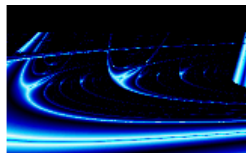


# Liquidity

## LIQUIDITY PROGRAMMING PARAMETERS

RATING	AVE VALUE TRADED PER MONTH (CALCULATED OVER 6 MONTHS)	PARAMETER	% DAYS TRADE	Liquidity Level
1	> R100 000 000	AND	>75%	High
2	> R30 000 000	AND	>75%	Normal
3	< R30 000 000	OR	<75%	Illiquid

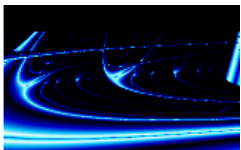
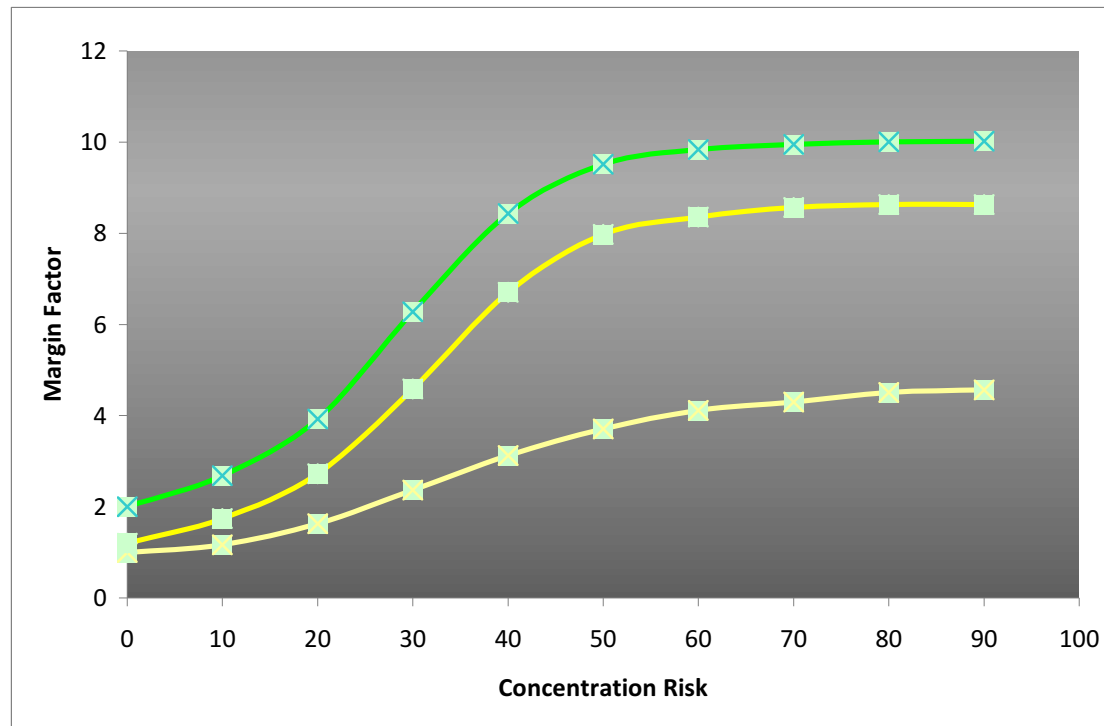
Liquidity and volatility.....



# Concentration Risk

Liquidity Rating	3	2	2.684521	3.928324	6.274398	8.433277	9.511071	9.835002	9.949161	10.00589	10.02
	2	1.2	1.742451	2.724644	4.584617	6.703902	7.974339	8.35733	8.567661	8.632931	8.63
	1	1	1.167901	1.628874	2.369143	3.125875	3.704345	4.114506	4.294166	4.507414	4.565
	0-10	10-20	20-30	30-40	40-50	50-60	60-70	70-80	80-90	90-100	

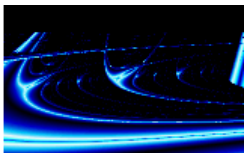
Concentration risk = Position / Shares in Issue



# SUCCESS

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- This solution was a quick AND very cheap one
- It did not require ANY IT system changes
- It works....why
- Due to higher margin requirements the volumes in the illiquids almost dried up...why
- Every trader is very cash sensitive... remember the currency futures....
- Solution: If one understands how the market operates and what is important, one might not need a complex highly involved solution!



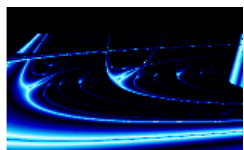
# Interest Rate Derivatives - Margins

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The Initial margin requirements (IMR) for the interest rate contracts are as follows and are effective, 8<sup>th</sup> March 2010.

<b>Contract Code</b>	<b>Expiry Date</b>	<b>Fixed Margin</b>	<b>Spread Margin</b>	<b>VSR</b>	<b>Series Spread Margin</b>
R155	06/05/2010	600	50	1.00	140
R157	06/05/2010	1370	70	1.00	100
R157	05/08/2010	1390	70	1.00	100
R157	04/11/2010	1390	70	1.00	100
R186	06/05/2010	2800	140	1.00	230
R186	05/08/2010	2850	140	1.00	230
R186	04/11/2010	2850	140	1.00	230

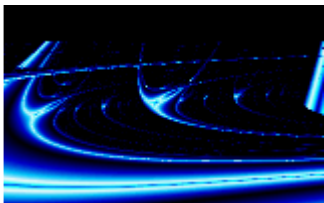
- Let's calculate margins.....



# Data Input: Problem 3

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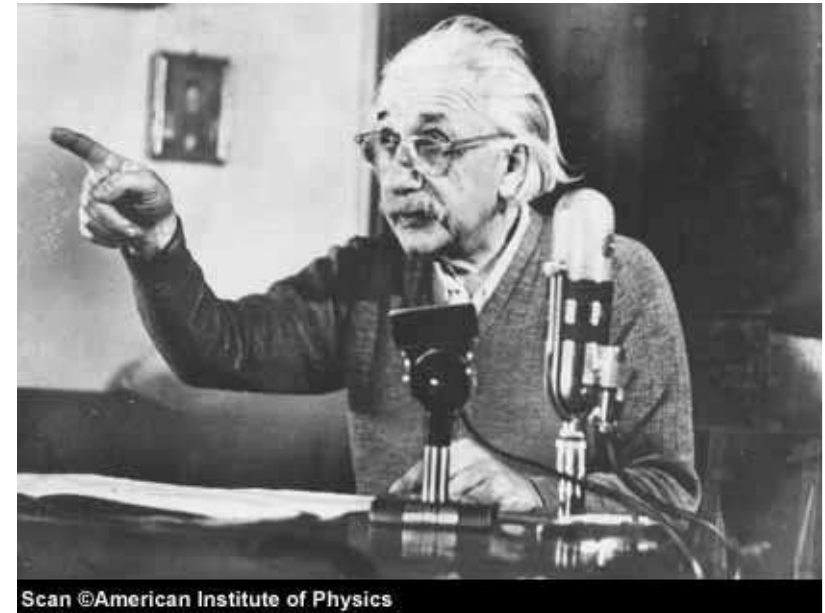
- Problem: what data should one use?
- NB: Bonds (and the futures) trade on YIELD but settle on ALL-IN-PRICE – AIP determines cash flows....
- Let's use the YTM's and AIP's..... - excel



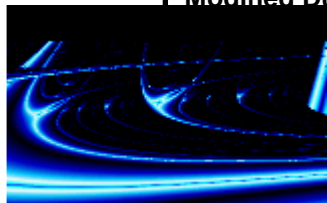
# Bond Duration

- What's the problem with this method (if any)?
- R157 matures on 15 Sep 2015
- Let's test something:

	Spot	Spot
Bond	r157	r157
Value date	15-Mar-10	15-Mar-05
YTM	8.180%	8.180%
Settlement date	18-Mar-10	18-Mar-05
All-in Price	123.270710	137.099730
Rand per Point	-497.6517586471	-864.9031999481
Rand per Point per Point	0.25895576	0.75339854
Duration	4.202180178279	6.566590098461
Modified Duration	4.037064250437	6.308569601750



- As time progresses the dynamics of a bond changes due to the changes in Rpp and duration

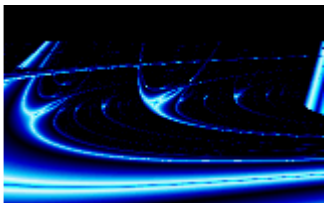


# Historical Time Series

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- Can we really use time series as we did in the calculation of standard deviations?
- Let's look at this problem from a different angle...
- There are two fundamental building blocks in the financial markets where resources are necessary to ensure they are implemented correctly

**Yield Curve** and **Volatility Surface**

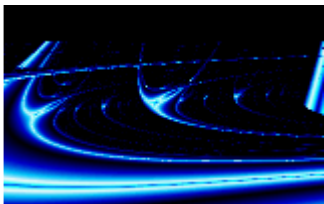




# Using the Yield Curve for Bond Futures

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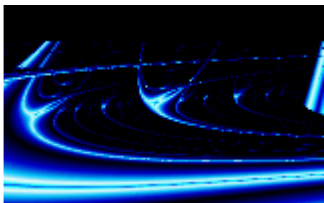
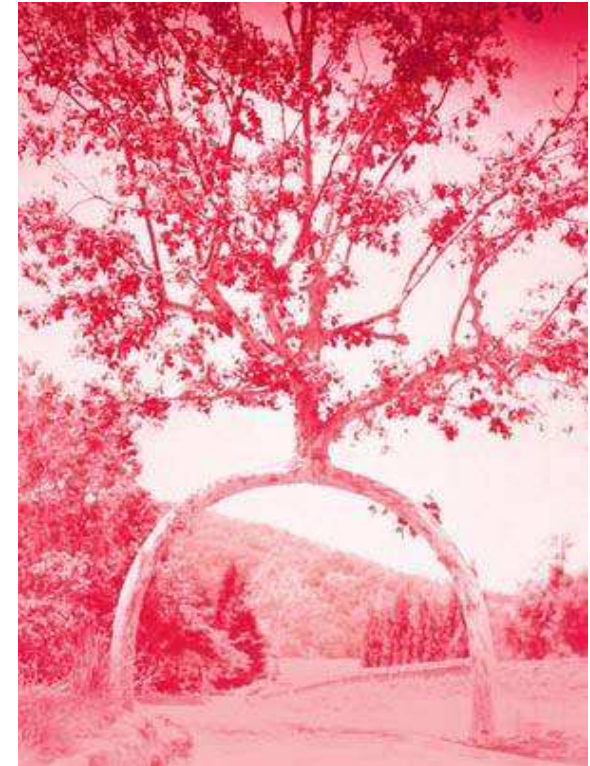
- Example: calculate a time series of R157 bond prices using the series of yield curves
- Use BESA's perfect fit bond yield curves from 28 Feb 2002...
- On 11 March the R157's MtM was 8.245% and an AIP of 122.89381
- Let's see what we can do with our yield curves...
- Using the yield curve gives a price of 122.69701
- Now we can calculate the margins using these "generated" time series... excel
- Problem solved!



## Using the Yield Curve with the Top 40 index: Problem 4

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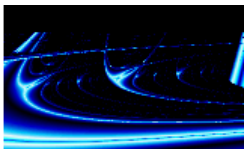
- Extension to equities: We can do exactly the same BUT using the Top 40 and relevant dividend yields to generate theoretical forward values... excel
- Most banks use the theoretical forward prices in their own mark-to-market calculations
- Safex currently mark-to-market near Alsi future, everything else is **marked-to-model**
- Not implemented yet, still in test phase



## Offsets: Problem 5

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- If a portfolio contains instruments that is correlated, a “rebate” is given to reflect the correlation
- Two types of offsets
  - Series spreads or calendar spread offsets e.g. going long a June Alsi and shorting a Sep Alsi
  - Group series offsets e.g. going long a May R157 futures and shorting a May R186 future
- Using correlation and covariance matrices.....excel
- Implemented for all interest rate futures
- Will extend later on to incorporate the Top 40 SSFs



# Options

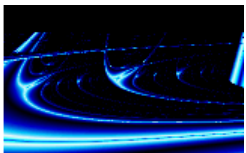
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- One extra source of risk: volatility
- We have the fixed margin and volatility surface so let's do some scenario analysis....excel

$$\frac{dS}{S} = \mu(t) dt + \sigma(t, S / K) dW$$

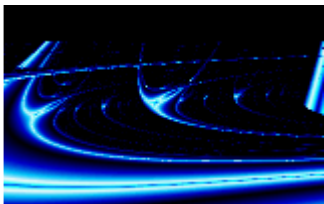
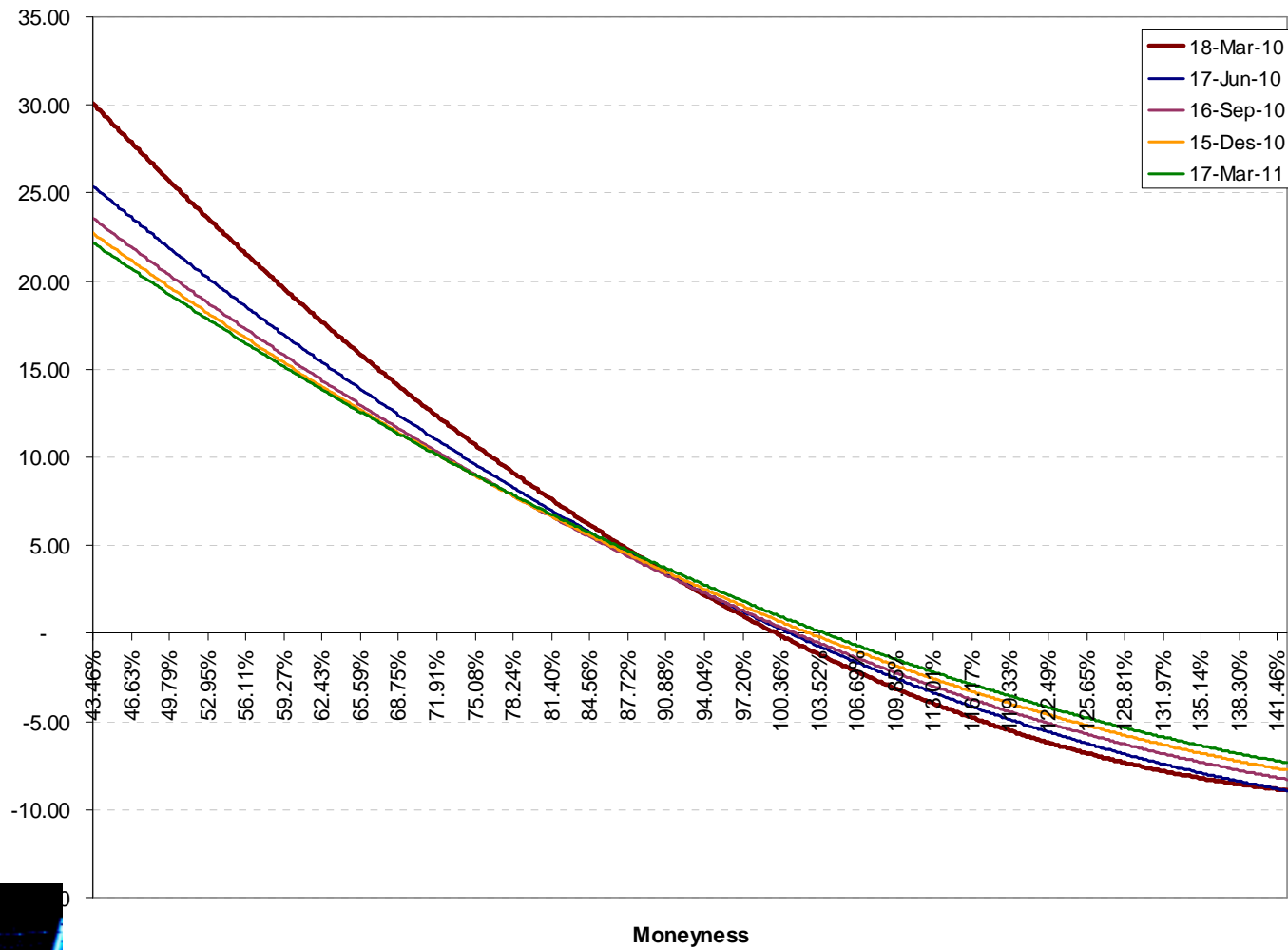


"Nurse, get on the internet, go to SURGERY.COM, scroll down and click on the 'Are you totally lost?' icon."



# Options: Current Alsi vol Surface

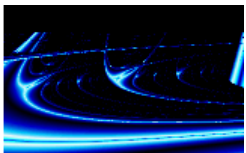
Alsi Volatility Surface on 9 Mar 2010



## Options - Can-Dos: Problem 6

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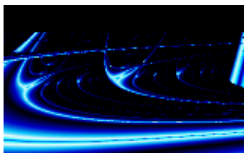
- How do we calculate the initial margin for exotic options?
- Use exactly the same method to calculate margins for exotic options
- Instead of calling BS model, call relevant exotic option model.....excel digital
- Biggest issue is how does one incorporate the volatility surface into the pricing equations?
- Most exotics discrete in time
- Even for options where closed form solutions exist, one needs to use numerical procedures
- Can now explain to any market player how the margins are calculated



## Options – VSR: Problem 7

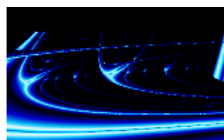
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- VSR = volatility scanning range
- Better to call it the volatility of volatility
- How much can the volatility change from today to tomorrow?
- Most volatility models has the vol of vol as input or it is calculated as part of the optimisation process when the volatility surface is generated
- It is in essence the curvature of the skew
- Can we use the **sticky strike** vol skew?
- Yes, it gives a much better reflection of the market's view on volatility the risk
- Safex uses it since September 2009 to update ATM vols



# Options: VSR

Expiry Date	MtM	Current ATM Vol	VolVol (v)	Max Volatility Change	Fixed Margin	Vol from Sticky Strike	Vol Change or VSR
18-Mar-10	25,308	23.00	32.539%	<b>7.48</b>	16500	25.409	2.41
17-Jun-10	25,594	23.00	23.143%	<b>5.32</b>	17000	25.184	2.18
16-Sep-10	25,718	23.00	21.053%	<b>4.84</b>	17000	25.018	2.02
15-Dec-10	26,014	23.50	19.893%	<b>4.67</b>	17000	25.407	1.91
17-Mar-11	26,322	23.50	19.083%	<b>4.48</b>	17500	25.379	1.88
15-Jun-11	26,658	23.50	18.486%	<b>4.34</b>	17500	25.308	1.81
15-Dec-11	27,314	23.75	17.602%	<b>4.18</b>	18000	25.496	1.75
15-Mar-12	27,568	23.75	17.264%	<b>4.10</b>	18000	25.453	1.70
20-Dec-12	28,808	24.25	16.465%	<b>3.99</b>	18500	25.862	1.61
18-Dec-14	32,308	24.25	15.207%	<b>3.69</b>	19000	25.631	1.38





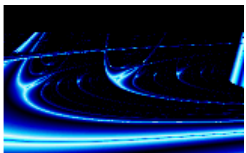
## Options: VSR Statistics

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- Can we calculate the “volatility change” for every fixed margin using historical skews to obtain a statistical VSR?
- Ja, but do not have that many skews – monthly skews from July 2008 and daily skews from July 2009
- What about Variance Swaps?
- Trading implied variance

$$Payoff_T = NumberContracts \times VPV \times [Realised\ Variance - K]$$

$$IMR = NumberContracts \times VPV \times [2\lambda\sqrt{K} + \lambda^2]$$



## Contact

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**Dr Antonie Kotzé**

**Email: [consultant@quantonline.co.za](mailto:consultant@quantonline.co.za)**

**Phone: 082 924-7162**

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